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OF SCIENCE AND TECHNOLOGY**

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| QUALIFICATION : BACHELOR OF SCIENCE HONOURS IN APPLIED STATISTICS | |
| QUALIFICATION CODE: 08BSHS | LEVEL: 8 |
| COURSE: SAMPLING THEORY | COURSE CODE: SAT802S |
| DATE: JANUARY 2025 | SESSION: 1 |
| DURATION: 3 HOURS | MARKS: 100 |

SECOND OPPORTUNITY / SUPPLEMENTARY: QUESTION PAPER

EXAMINER: *Mr. Jan Johannes Swartz*

MODERATOR: *Prof. Opeoluwa Oyedele*

INSTRUCTIONS:

1. Answer all questions on the separate answer sheet.
2. Please write neatly and legibly.
3. Do not use the left side margin of the exam paper. This must be allowed for the examiner.
4. No books, notes and other additional aids are allowed.
5. Mark all answers clearly with their respective question numbers.

PERMISSIBLE MATERIALS:

1. Non-Programmable Calculator

ATTACHMENTS

1. Z - Table
2. T - Table

This paper consists of 4 pages including this front page

Question 1 [25 marks]

- 1.1. What is meant by the sampling distribution of a statistic? [5]
- 1.2. Select all the 20 samples of size three from the population of six students in Table 2.1, below without replacement.
- 1.2.1 From each sample, find the 95% confidence limits for the population mean of the math scores with the known population variance and its estimates; use the normal deviate $Z = 1.96$ in both cases. [10]
- 1.2.2 Compare the average of the confidence widths obtained with the estimates of variance with the exact width for the case of known variance. [10]

Table 2.1. SAT verbal and math scores.

| Student i | Verbal x_i | Math y_i |
|----------------|-----------------|---------------|
| 1 | 520 | 670 |
| 2 | 690 | 720 |
| 3 | 500 | 650 |
| 4 | 580 | 720 |
| 5 | 530 | 560 |
| 6 | 480 | 700 |
| Total | 3300 | 4020 |
| Mean | 550 | 670 |
| Variance | | |
| σ^2 | 4866.67 | 3066.67 |
| S^2 | 5840 | 3680 |
| S | 76.42 | 60.66 |
| C.V. (%) | 13.89 | 9.05 |

C.V. = coefficient of variation.

Question 2 [28 marks]

- 2.1. Provide and explain four basic criteria for the acceptability of a sampling method? [8]
- 2.2. The investigator samples 10 one-acre plots by simple random sampling and counts the number of trees (y) on each plot. She also has aerial photographs of the plantation from which she can estimate the number of trees (x) on each plot of the entire plantation. Hence, she knows $\mu_x = 19.7$ and since the two counts are approximately proportional through the origin, she uses a ratio estimate to estimate μ_y

Table 1: To estimate the average number of trees per acre on a 1000- acre plantation

| Plot | Actual no. per acre Y | Aerial estimate X | $y_i - rx_i$ |
|------|-----------------------|-------------------|--------------|
| 1 | 25 | 23 | 0.5625 |
| 2 | 15 | 14 | 0.1250 |
| 3 | 22 | 20 | 0.7500 |
| 4 | 24 | 25 | -2.5625 |
| 5 | 13 | 12 | 0.2500 |
| 6 | 18 | 18 | -1.1250 |
| 7 | 35 | 30 | 3.1250 |
| 8 | 30 | 27 | 1.3125 |
| 9 | 10 | 8 | 1.5000 |
| 10 | 29 | 31 | -3.9375 |
| mean | 22.10 | 20.80 | - |

2.2.1. Study Figures 1 and 2 and discuss the suitability of using ratio estimates. [5]

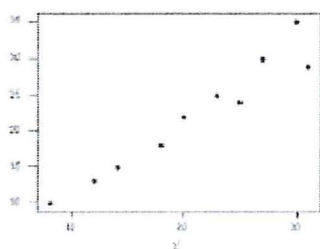


Figure 1: Scatter plot

The regression equation is
 $Y = 1.04 + 1.00 X$

| Predictor | Coef | SE Coef | T | P |
|-----------|---------|---------|-------|-------|
| Constant | 1.039 | 0.007 | 0.62 | 0.554 |
| X | 1.00193 | 0.00094 | 11.03 | 0.000 |

Figure 2: Regression output

2.2.2. Construct the approximate 95% confidence interval for μ_y [15]

Question 3 [17 marks]

3.1. The New York Times of February 25, 1994, summarized the results of a survey conducted by Klein Associates, Inc. on 2000 lawyers on sexual advances in the office. Between 85 and 98% responded to the questions in the survey; 49% of the responding women and 9% of the responding men agreed that some sorts of harassment exist in the offices. Assume that the population of lawyers is large and there are equal numbers of female and male lawyers, and ignore the nonresponse; that is, consider the respondents to be a random sample of the 2000 lawyers.

3.1.1 Find the standard errors for females and males. [5]

3.2. To estimate the percentage of people that carries a viral infection which produces AIDS, 128 people are examined and 72 of them are found to be infected. Calculate the standard error of the estimated proportion and compute a 95% confidence interval for the population proportion? [7]

3.3. If no information of P (proportion) is provided when determining the sample size of a population, find the error of the estimation e for $n = 2000$, Consider $\alpha = 0.05$ for both cases. [5]

Question 4 [30 marks]

4.1. [10]

Let there exist a population $U = \{1, 2, 3\}$ with the following design:

$$p(\{1, 2\}) = \frac{1}{2}, p(\{1, 3\}) = \frac{1}{4}, p(\{2, 3\}) = \frac{1}{4}.$$

Give the first-order inclusion probabilities. Give the variance-covariance matrix Δ of indicator variables for inclusion in the sample. Give the variance matrix of the unbiased estimator for the total.

4.2. Between the 100 computer corporations in Namibia, the average of employee sizes for the largest 10 and smallest 10 corporations were known to be 300 and 100, respectively. For a sample of 20 from the remaining 80 corporations, the mean and standard deviation were 250 and 110, respectively. For the total employee size of the 80 corporations, find the

- a) Estimate of the total, [3]
- b) Standard error of the estimate, and [3]
- c) 95% confidence limits. [5]

4.3. Write a short description on the importance of the normal distribution in sampling theory [5]

4.4. List 4 properties of the normal probability distribution. [4]

*****END OF EXAMINATION*****

Standard Normal Probabilities

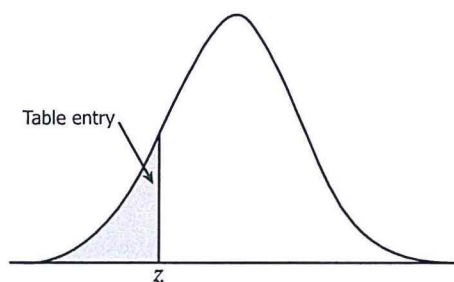


Table entry for z is the area under the standard normal curve to the left of z .

| z | .00 | .01 | .02 | .03 | .04 | .05 | .06 | .07 | .08 | .09 |
|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| -3.4 | .0003 | .0003 | .0003 | .0003 | .0003 | .0003 | .0003 | .0003 | .0003 | .0002 |
| -3.3 | .0005 | .0005 | .0005 | .0004 | .0004 | .0004 | .0004 | .0004 | .0004 | .0003 |
| -3.2 | .0007 | .0007 | .0006 | .0006 | .0006 | .0006 | .0006 | .0005 | .0005 | .0005 |
| -3.1 | .0010 | .0009 | .0009 | .0009 | .0008 | .0008 | .0008 | .0008 | .0007 | .0007 |
| -3.0 | .0013 | .0013 | .0013 | .0012 | .0012 | .0011 | .0011 | .0011 | .0010 | .0010 |
| -2.9 | .0019 | .0018 | .0018 | .0017 | .0016 | .0016 | .0015 | .0015 | .0014 | .0014 |
| -2.8 | .0026 | .0025 | .0024 | .0023 | .0023 | .0022 | .0021 | .0021 | .0020 | .0019 |
| -2.7 | .0035 | .0034 | .0033 | .0032 | .0031 | .0030 | .0029 | .0028 | .0027 | .0026 |
| -2.6 | .0047 | .0045 | .0044 | .0043 | .0041 | .0040 | .0039 | .0038 | .0037 | .0036 |
| -2.5 | .0062 | .0060 | .0059 | .0057 | .0055 | .0054 | .0052 | .0051 | .0049 | .0048 |
| -2.4 | .0082 | .0080 | .0078 | .0075 | .0073 | .0071 | .0069 | .0068 | .0066 | .0064 |
| -2.3 | .0107 | .0104 | .0102 | .0099 | .0096 | .0094 | .0091 | .0089 | .0087 | .0084 |
| -2.2 | .0139 | .0136 | .0132 | .0129 | .0125 | .0122 | .0119 | .0116 | .0113 | .0110 |
| -2.1 | .0179 | .0174 | .0170 | .0166 | .0162 | .0158 | .0154 | .0150 | .0146 | .0143 |
| -2.0 | .0228 | .0222 | .0217 | .0212 | .0207 | .0202 | .0197 | .0192 | .0188 | .0183 |
| -1.9 | .0287 | .0281 | .0274 | .0268 | .0262 | .0256 | .0250 | .0244 | .0239 | .0233 |
| -1.8 | .0359 | .0351 | .0344 | .0336 | .0329 | .0322 | .0314 | .0307 | .0301 | .0294 |
| -1.7 | .0446 | .0436 | .0427 | .0418 | .0409 | .0401 | .0392 | .0384 | .0375 | .0367 |
| -1.6 | .0548 | .0537 | .0526 | .0516 | .0505 | .0495 | .0485 | .0475 | .0465 | .0455 |
| -1.5 | .0668 | .0655 | .0643 | .0630 | .0618 | .0606 | .0594 | .0582 | .0571 | .0559 |
| -1.4 | .0808 | .0793 | .0778 | .0764 | .0749 | .0735 | .0721 | .0708 | .0694 | .0681 |
| -1.3 | .0968 | .0951 | .0934 | .0918 | .0901 | .0885 | .0869 | .0853 | .0838 | .0823 |
| -1.2 | .1151 | .1131 | .1112 | .1093 | .1075 | .1056 | .1038 | .1020 | .1003 | .0985 |
| -1.1 | .1357 | .1335 | .1314 | .1292 | .1271 | .1251 | .1230 | .1210 | .1190 | .1170 |
| -1.0 | .1587 | .1562 | .1539 | .1515 | .1492 | .1469 | .1446 | .1423 | .1401 | .1379 |
| -.9 | .1841 | .1814 | .1788 | .1762 | .1736 | .1711 | .1685 | .1660 | .1635 | .1611 |
| -.8 | .2119 | .2090 | .2061 | .2033 | .2005 | .1977 | .1949 | .1922 | .1894 | .1867 |
| -.7 | .2420 | .2389 | .2358 | .2327 | .2296 | .2266 | .2236 | .2206 | .2177 | .2148 |
| -.6 | .2743 | .2709 | .2676 | .2643 | .2611 | .2578 | .2546 | .2514 | .2483 | .2451 |
| -.5 | .3085 | .3050 | .3015 | .2981 | .2946 | .2912 | .2877 | .2843 | .2810 | .2776 |
| -.4 | .3446 | .3409 | .3372 | .3336 | .3300 | .3264 | .3228 | .3192 | .3156 | .3121 |
| -.3 | .3821 | .3783 | .3745 | .3707 | .3669 | .3632 | .3594 | .3557 | .3520 | .3483 |
| -.2 | .4207 | .4168 | .4129 | .4090 | .4052 | .4013 | .3974 | .3936 | .3897 | .3859 |
| -.1 | .4602 | .4562 | .4522 | .4483 | .4443 | .4404 | .4364 | .4325 | .4286 | .4247 |
| 0.0 | .5000 | .4960 | .4920 | .4880 | .4840 | .4801 | .4761 | .4721 | .4681 | .4641 |

Standard Normal Probabilities

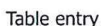
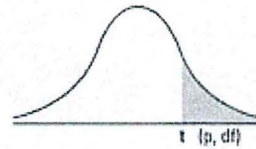


Table entry for z is the area under the standard normal curve to the left of z .

[illegible]

Numbers in each row of the table are values on a t -distribution with (df) degrees of freedom for selected right-tail (greater-than) probabilities (p).



| df/p | 0.40 | 0.25 | 0.10 | 0.05 | 0.025 | 0.01 | 0.005 | 0.0005 |
|------|----------|----------|----------|----------|----------|----------|----------|----------|
| 1 | 0.324920 | 1.000000 | 3.077684 | 6.313752 | 12.70620 | 31.82052 | 63.65674 | 636.6192 |
| 2 | 0.288675 | 0.816497 | 1.885618 | 2.919986 | 4.30265 | 6.96456 | 9.92484 | 31.5991 |
| 3 | 0.276671 | 0.764892 | 1.637744 | 2.353363 | 3.18245 | 4.54070 | 5.84091 | 12.9240 |
| 4 | 0.270722 | 0.740697 | 1.533206 | 2.131847 | 2.77645 | 3.74695 | 4.60409 | 8.6103 |
| 5 | 0.267181 | 0.726687 | 1.475884 | 2.015048 | 2.57058 | 3.36493 | 4.03214 | 6.8688 |
| 6 | 0.264835 | 0.717558 | 1.439756 | 1.943180 | 2.44691 | 3.14267 | 3.70743 | 5.9588 |
| 7 | 0.263167 | 0.711142 | 1.414924 | 1.894579 | 2.36462 | 2.99795 | 3.49948 | 5.4079 |
| 8 | 0.261921 | 0.706387 | 1.396815 | 1.859548 | 2.30600 | 2.89646 | 3.35539 | 5.0413 |
| 9 | 0.260955 | 0.702722 | 1.383029 | 1.833113 | 2.26216 | 2.82144 | 3.24984 | 4.7809 |
| 10 | 0.260185 | 0.699812 | 1.372184 | 1.812461 | 2.22814 | 2.76377 | 3.16927 | 4.5869 |
| 11 | 0.259556 | 0.697445 | 1.363430 | 1.795885 | 2.20099 | 2.71808 | 3.10581 | 4.4370 |
| 12 | 0.259033 | 0.695483 | 1.356217 | 1.782288 | 2.17881 | 2.68100 | 3.05454 | 4.3178 |
| 13 | 0.258591 | 0.693829 | 1.350171 | 1.770933 | 2.16037 | 2.65031 | 3.01228 | 4.2208 |
| 14 | 0.258213 | 0.692417 | 1.345030 | 1.761310 | 2.14479 | 2.62449 | 2.97684 | 4.1405 |
| 15 | 0.257885 | 0.691197 | 1.340606 | 1.753050 | 2.13145 | 2.60248 | 2.94671 | 4.0728 |
| 16 | 0.257599 | 0.690132 | 1.336757 | 1.745884 | 2.11991 | 2.58349 | 2.92078 | 4.0150 |
| 17 | 0.257347 | 0.689195 | 1.333379 | 1.739607 | 2.10982 | 2.56693 | 2.89823 | 3.9651 |
| 18 | 0.257123 | 0.688364 | 1.330391 | 1.734064 | 2.10092 | 2.55238 | 2.87844 | 3.9216 |
| 19 | 0.256923 | 0.687621 | 1.327728 | 1.729133 | 2.09302 | 2.53948 | 2.86093 | 3.8834 |
| 20 | 0.256743 | 0.686954 | 1.325341 | 1.724718 | 2.08596 | 2.52798 | 2.84534 | 3.8495 |
| 21 | 0.256580 | 0.686352 | 1.323188 | 1.720743 | 2.07961 | 2.51765 | 2.83136 | 3.8193 |
| 22 | 0.256432 | 0.685805 | 1.321237 | 1.717144 | 2.07387 | 2.50832 | 2.81876 | 3.7921 |
| 23 | 0.256297 | 0.685306 | 1.319460 | 1.713872 | 2.06866 | 2.49987 | 2.80734 | 3.7676 |
| 24 | 0.256173 | 0.684850 | 1.317836 | 1.710882 | 2.06390 | 2.49216 | 2.79694 | 3.7454 |
| 25 | 0.256060 | 0.684430 | 1.316345 | 1.708141 | 2.05954 | 2.48511 | 2.78744 | 3.7251 |
| 26 | 0.255955 | 0.684043 | 1.314972 | 1.705618 | 2.05553 | 2.47863 | 2.77871 | 3.7066 |
| 27 | 0.255858 | 0.683685 | 1.313703 | 1.703288 | 2.05183 | 2.47266 | 2.77068 | 3.6896 |
| 28 | 0.255768 | 0.683353 | 1.312527 | 1.701131 | 2.04841 | 2.46714 | 2.76326 | 3.6739 |
| 29 | 0.255684 | 0.683044 | 1.311434 | 1.699127 | 2.04523 | 2.46202 | 2.75639 | 3.6594 |
| 30 | 0.255605 | 0.682756 | 1.310415 | 1.697261 | 2.04227 | 2.45726 | 2.75000 | 3.6460 |
| z | 0.253347 | 0.674490 | 1.281552 | 1.644854 | 1.95996 | 2.32635 | 2.57583 | 3.2905 |
| CI | ——— | ——— | 80% | 90% | 95% | 98% | 99% | 99.9% |