



Faculty of Health, Natural Resources and Applied Sciences

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QUALIFICATION: BACHELOR OF SCIENCE IN APPLIED MATHEMATICS AND STATISTICS & BACHELOR OF SCIENCE			
QUALIFICATION CODE:	07BSAM, & 07BSOC	LEVEL:	5
COURSE:	CALCULUS 1	COURSE CODE:	CLS502S
DATE:	JANUARY 2025	SESSION:	2
DURATION:	3 HOURS	MARKS:	100

SECOND OPPORTUNITY/SUPPLEMENTARY EXAMINATION: QUESTION PAPER

EXAMINER:

Dr. David liyambo

MODERATOR:

Dr. Nega Chere

INSTRUCTIONS:

- 1. Attempt all the questions in the booklet provided.
- 2. Please write neatly and legibly using a black or blue inked pen, and sketches must be done in pencil.
- 3. Do not use the left side margin of the answer script. This must be allowed for the examiner.
- 4. No books, notes or other additional aids are allowed.
- 5. Mark all answers clearly with their respective question numbers.
- 6. Show clearly all the steps used in the calculations.

PERMISSIBLE MATERIALS:

1. Non-programmable calculator without a cover.

ATTACHMENTS:

None

This paper consists of 3 pages including this front page

Question 1.

The functions f, g and h are defined by, $f(x)=\dfrac{2x+1}{\sqrt{x^2+5x+4}}$, $g(x)=x^2+3$ and h(x)=2x+a.

- a) Find the domain of f. [6]
- **b)** Given that $(g \circ h)(x) = 4x^2 8x + 7$, where $x \neq 0$, calculate the value of a. [5]

Question 2.

2.1 Find the following limits, if they exist.

a)
$$\lim_{h \to 0} \frac{\sqrt{4+h}-2}{h}$$
. [7]

b)
$$\lim_{x\to 2^-} \frac{x^2-4}{|x-2|}$$
 [6]

c)
$$\lim_{x \to 0^+} (e^x + x)^{\frac{1}{x}}$$
 [8]

d)
$$\lim_{x \to 3} \frac{1}{(3-x)^2}$$
. [4]

2.2 Using the Precise definition (the $\varepsilon-\delta$ method), prove that $\lim_{x\to -3}(14-5x)=29.$ [9]

Question 3.

- a) Use the definition (first principle) to find the derivative of $f(x) = \sqrt{x+1}$. [10]
- b) Find the equation of the tangent line to the graph of f at the point where x=3. [5]
- c) Find g'(x) for each of the following functions.

(i)
$$g(x) = \cos^2(\cos x)$$
 [5]

(ii)
$$g(x) = 3^x e^x$$

Question 4.

Consider the function $f(x) = \left\{ \begin{array}{ll} x-m & \text{if } x < 3; \\ 1-mx & \text{if } x \geq 3. \end{array} \right.$

- a) Find the value of m for which f is a continuous function at x=3. [9]
- b) With the value of m you found in a), is f differentiable at x=3 or not? Justify your answer.

[5]

Question 5.

Let $f(x) = x^{\frac{1}{3}}(2x+7)$ and $g(x) = 2x - 3x^{\frac{2}{3}}$.

- a) Find the intervals on which f is increasing and on which it is decreasing, and hence state the local extreme values of f. If you answer is not a whole number, round it correct to 2 decimal places. [10]
- b) Find the intervals on which the graph of y=g(x) is concave upwards and on which it is concave downwards. [7]

END OF EXAMINATION QUESTION PAPER