NAMIBIA UNIVERSITY
OF SCIENCE AND TECHNOLOGY

FACULTY OF COMMERCE, HUMAN SCIENCES AND EDUCATION

DEPARTMENT OF MARKETING, LOGISTICS AND SPORT MANAGEMENT

QUALIFICATION: POST GRADUATE DIPLOMA IN PROCUREMENT MANAGEMENT	
QUALIFICATION CODE: 08PDPM	**LEVEL:** 8
COURSE CODE: FTP801S	**COURSE NAME:** FINANCIAL TECHNIQUES FOR PROCUREMENT AND SUPPLY CHAIN MANAGEMENT
SESSION: APRIL 2024	**PAPER:** THEORY AND CALCULATIONS
DURATION: 3 HOURS	**MARKS:** 100

FIRST OPPORTUNITY FINAL ASSESSMENT QUESTION PAPER	
EXAMINER	MR. LAMECK ODADA
MODERATOR	MR. JOHANNES NDJULUWA

INSTRUCTIONS

1. This question paper consists of **FOUR (4)** questions.
2. Answer **ALL FOUR (4)** questions in blue or black ink only. **NO PENCIL.**
3. Start each question on a new page, number the answers correctly and clearly.
4. Write clearly, neatly and show all your workings/calculations/assumptions.
5. Unless otherwise stated, work with four (4) decimal places in all your calculations and only round off final answers to two (2) decimal places.
6. Questions relating to this assessment may be raised in the initial 30 minutes after the start of the examination. Thereafter, candidates must use their initiative to deal with any perceived error or ambiguities and any assumptions made by the candidate should be clearly stated.

PERMISSIBLE MATERIALS

- Silent, non-programmable calculators

THIS FINAL ASSESSMENT CONSISTS OF _9_ PAGES (including this cover page, not tables)

QUESTION 1 **[20 MARKS]**

For questions 1.1 – 1.10, write only the answer (the correct letter chosen) in your answer book and not on the question paper. Do not copy the question again. **(2 marks each)**

1.1 Capital rationing comes about because:

a) There are not enough positive NPV projects

b) Companies do not always have access to all the funds they could make use of

c) Managers find it difficult to decide how to fund projects

d) Banks require very high returns on projects

1.2 In cases where capital must be rationed, a firm should rank projects according to their

a) net present values.

b) internal rates of return.

c) profitability indexes.

d) external rates of return.

1.3 Asymmetric information refers to circumstances in which.

a) both parties to a transaction have identical amounts of information.

b) neither party to a transaction has any relevant information.

c) one party to a transaction has more information than the other party.

d) the riskiness of a transaction is greater than its expected return.

1.4 The principal-agent problem may result if

a) a firm is owned and operated by the same person.

b) managers make decisions that are not in the best interest of owners.

c) a firm compensates managers based on the profitability of the firm.

d) All of the above.

1.5 One way to correct a potential principal-agent problem is for stockholders to

a) offer managers "golden parachutes" in the event of a takeover.

b) empower managers to make the decisions they feel are best.

c) ensure that there is no explicit linkage between managers' compensation and the profitability of the firm.

d) All of the above.

1.6 The coefficient of variation measures

a) the risk per unit of expected payoff.

b) the risk-adjusted expected value.

c) the payoff per unit of risk.

d) a decision maker's risk-return trade-off.

1.7 Which of the following items describes an index measure of systematic risk?

a) Beta.

b) Standard deviation.

c) Coefficient of variation.

d) Variance.

1.8 This type of risk is avoidable through proper diversification.

a) portfolio risk

b) systematic risk

c) unsystematic risk

d) total risk

1.9 The term "capital structure" refers to:

a) long-term debt, preferred stock, and common stock equity.

b) current assets and current liabilities.

c) total assets minus liabilities.

d) shareholders' equity.

1.10 The after-tax weighted average cost of capital is determined by:

a) Multiplying the weighted average after tax cost of debt by the weighted average cost of equity

b) Adding the weighted average before tax cost of debt to the weighted average cost of equity

c) Adding the weighted average after tax cost of debt to the weighted average cost of equity

d) Dividing the weighted average before tax cost of debt to the weighted average cost of equity

(2 marks each, 2 x 10 = 20 marks)

QUESTION 2 **[30 MARKS]**

Amagulu Group of companies (hereafter Amagulu) is made up of companies with various business portfolios. The Group is multifunctional and multidimensional, with subsidiaries and associates that can provide and sustain the provision of the basic needs and equipment to the Namibian nation at large. It prides itself as a group of wholly Namibian companies with the right personnel, expertise, and ability to procure equipment and render services efficiently.

Amagulu is evaluating an investment proposal to manufacture Product W33, which has performed well in test marketing trials conducted recently by the company's research and development division. The following information relating to investment proposal has now been prepared.

Initial investment	N$2 million
Selling price (current price terms)	N$20 per unit
Variable operating costs (current price terms)	N$8 per unit
Fixed operating costs (current price terms)	N$170,000 per year

The research and development division has prepared the following demand forecast as a result of its test marketing trials. The forecast reflects expected technological change and its effect on the anticipated life cycle of Product W33.

Year	1	2	3	4
Demand (units)	60,000	70,000	120,000	45,000

It is expected that all units of Product W33 produced will be sold, in line with the company's policy of keeping no inventory of finished goods. No machinery scrap value is expected at the end of four years, when production of Product W33 is planned to end. For investment appraisal, Amagulu uses a discount rate of 10% per year and a target return on capital employed of 30% per year. Ignore taxation.

REQUIRED		**MARKS**
a)	Identify any FOUR (4) factors that Amagulu should consider in evaluating this investment proposal	**4**
b)	Calculate the Net Present Value (NPV) for the investment proposal and advise whether the investment proposal is financially acceptable.	**14**
c)	Using a 17% cost of capital, calculate the Internal Rate of Return (IRR) for the investment proposal and advise whether the investment proposal is financially acceptable. ***Answer to the nearest whole number.***	**7**

d)	Calculate the Return on Capital Employed (ROCE)/Accounting Rate of Return (ARR) for the investment proposal and advise whether the investment proposal is financially acceptable. ***Answer to the nearest whole number.***	**5**
TOTAL		**30**

QUESTION 3 **[25 MARKS]**

Oshikoto Country Lodges (hereafter OCL) is a truly Namibian hospitality company. They provide their guests with unmatched experiences at unique properties with a true sense of place in the landscape. Staying at one of their lodges is a once-in-a-lifetime experience that is grounded in genuine, warm hospitality and a love of the land they come from. Developing a passionate and dedicated team is foremost in their philosophy, as only a great team can provide their guests with a first-class experience. They continually pursue excellence by enhancing our skills and evolving with the hospitality and tourism industry of Namibia. OCL is looking to expand its hospitality and tourism interest in Namibia by investing in two companies in the hospitality and tourism sector. OCL can invest N$4 million in one of the two companies or a portfolio of the two companies. The following risk/return profiles have been provided.

		Estimated Returns (%)		
Economic State	**Probability (%)**	**SLM Safaris**	**ATI Holidays**	**Market**
Recession	30	2	25	-
Boom	50	10	22	-
Depression	20	12	-2	-
Expected return		-	-	12%
Standard deviation		-	-	6%
Covariance with the market		25.2	39.6	-
The risk-free rate is 3% per annum and there is no company or personal taxation.				

REQUIRED		**MARKS**
a)	Calculate the expected returns together with the risk of SLM Safaris and ATI Holidays.	**6**
b)	If OCL is to select only one company to invest in, which one would you advise OCL to select? Motivate your answer with appropriate calculations.	**3**

c)	Determine the expected return of the portfolio, assuming that OCL invests N$1.6 million in SLM Safaris.	2
d)	Determine the covariance of SLM Safaris and ATI Holidays and interpret your answer.	4
e)	Determine the standard deviation of the portfolio and advise OCL on whether to invest in the portfolio or not.	6
f)	Calculate the required return for both companies according to the Capital Asset Pricing Model (CAPM)	4
TOTAL		**25**

QUESTION 4 **[25 MARKS]**

Dineo Manufacturing and Supplies (hereafter DMS) is a 100% Namibian custom garment manufacturer, founded in 2009 and started with operations in 2010. The target audience of DMS is corporate companies, public services, and schools and is not limited to local and international brands. Below is the summarized statement of the financial position of DMS and the statement of comprehensive income for the year ended 31 December 2023.

DMS Statement of financial position as of 31 December 2023

ASSETS	**2023**	**2022**
Non-current assets	9 450 000	8 640 000
Property, plant, and equipment	9 450 000	8 640 000
Investments	-	-
Current assets	36 045 000	29 632 500
Inventories	20 925 000	14 850 000
Receivables	12 150 000	9 990 000
Cash assets	2 970 000	4 792 500
TOTAL ASSETS	**45 495 000**	**38 272 500**
EQUITY AND LIABILITIES		
Share capital and reserves	16 335 000	15 120 000
Share capital	7 000 000	7 000 000
Other reserves	-250 000	-250 000
Retained earnings	9 585 000	8 370 000
Redeemable -preference shares	2 700 000	2 700 000
Non-current liabilities: Long-term borrowings	7 425 000	7 425 000
Current liabilities	**19 035 000**	**13 027 500**

Trade and other payables	4 860 000	4 320 000
Short term borrowings	14 175 000	8 707 500
TOTAL EQUITY AND LIABILITIES	**45 495 000**	**38 272 500**

DMS Statement of comprehensive income for the year ended 31 December 2023

	2023	**2022**
Sales	85 320 000	74 250 000
Cost of sales	63 990 000	54 945 000
Gross profit	**21 330 000**	**19 305 000**
Operating expenses	12 636 000	11 070 000
Depreciation	810 000	675 000
Profit before interest and tax	**7 884 000**	**7 560 000**
Finance costs	2 430 000	1 485 000
Profit before tax	**5 454 000**	**6 075 000**
Income tax expense	2 430 000	2 160 000
Profit from continuing operations	**3 024 000**	**3 915 000**
loss on discontinued operations	1 080 000	-
Profit for the year	**1 944 000**	**3 915 000**

DMS Statement of changes in equity for the year ended 31 December 2023

	2023	**2022**
Balance on 31 December	8 370 000	5 184 000
Comprehensive income for the year	1 944 000	3 915 000
	10 314 000	9 099 000
Dividends-preference shares	-324 000	-324 000
Dividends-ordinary shares	-405 000	-405 000
Balance on 31 December	9 585 000	8 370 000

REQUIRED		**MARKS**
a)	Compute the following liquidity ratios for 2022 and 2023 and comment on the overall liquidity position of DMS. • Current ratio • Quick ratio • Debtors' collection period • Creditors settlement period	**10**
b)	Compute the debt ratio of DMS for 2022 and 2023 and comment on your answer. • Debt ratio	**4**

c)	Compute the following profitability ratios for 2022 and 2023 and comment on the overall profitability of DMS. • Gross profit margin • Net profit margin • Return on Assets	**8**
d)	Explain any three (3) limitations of financial statement/ratio analysis	**3**
TOTAL		**25**

END OF QUESTION PAPER

FORMULA SHEET

Portfolio Expected Return	$ER_p = \sum W_A \times ER_A + W_B \times ER_B$
Portfolio standard deviation	$\sigma_{AB} = \sqrt{W_A^2 x \sigma^2_A + W_B^2 x \sigma^2_B + 2 x W_A x W_B x Cov_{AB}}$
Beta (β)	Covariance of company with market)/variance of market
Cost of equity capital	$R_e = Rf + \beta (Rm - Rf)$ and $R_e = [D_1 \div P_o] + g$
Before tax cost of debt	$k_d = I + [Par\ value - N_d]/n \div [N_d + par\ value]/2$
Frequency of compounding	$FV = PV[1 + (r/m)]^{t*m}$
Effective Annual Rate	$FV = PV[1 + (r/m)]^{t*m}$
Payment	$PMT = PV \times r/[1-1/(1+r)^t]$
Internal Rate of Return	$IRR = R_1 + [N_1 \times (R_2-R_1)]/N_1+N_2$
Profitability Index	$\frac{\text{Present value of future cash flows } (excluding\ initial\ outlay)}{\text{Initial investment}}$
Profitability Index	$1 + \frac{NPV}{\text{Initial investment}}$
Accounting Rate of Return	$\frac{\text{Average annual profit}}{\text{Average investment}}$
Expected return (discrete distribution)	$\sum P_i \times R_i$
Expected return (continuous distribution)	$\frac{\sum R_i}{N}$
Standard deviation (discrete distribution)	$\sqrt{\sum [R_i - E(R)]^2 x (P_i)}$
Standard deviation (continuous distribution)	$\sqrt{\frac{\sum (R_i - E(R)^2}{n}}$
Covariance (discrete distribution)	$= \Sigma Pi [R_A - E(R_A)] [R_B - E(R_B)]$
Coefficient of variation	$= \frac{\text{Standard deviation}}{\text{Expected return}}$
Correlation coefficient	$= \frac{\text{Covariance of the assets 1 and 2}}{\sigma_1 x \sigma_2}$

TABLE A

Future value interest factor of $1 per period at i% for n periods, FVIF(i,n).

Period	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	11%	12%	13%	14%	15%	16%	17%	18%	19%	20%
1	1.010	1.020	1.030	1.040	1.050	1.060	1.070	1.080	1.090	1.100	1.110	1.120	1.130	1.140	1.150	1.160	1.170	1.180	1.190	1.200
2	1.020	1.040	1.061	1.082	1.103	1.124	1.145	1.166	1.188	1.210	1.232	1.254	1.277	1.300	1.323	1.346	1.369	1.392	1.416	1.440
3	1.030	1.061	1.093	1.125	1.158	1.191	1.225	1.260	1.295	1.331	1.368	1.405	1.443	1.482	1.521	1.561	1.602	1.643	1.685	1.728
4	1.041	1.082	1.126	1.170	1.216	1.262	1.311	1.360	1.412	1.464	1.518	1.574	1.630	1.689	1.749	1.811	1.874	1.939	2.005	2.074
5	1.051	1.104	1.159	1.217	1.276	1.338	1.403	1.469	1.539	1.611	1.685	1.762	1.842	1.925	2.011	2.100	2.192	2.288	2.386	2.488
6	1.062	1.126	1.194	1.265	1.340	1.419	1.501	1.587	1.677	1.772	1.870	1.974	2.082	2.195	2.313	2.436	2.565	2.700	2.840	2.986
7	1.072	1.149	1.230	1.316	1.407	1.504	1.606	1.714	1.828	1.949	2.076	2.211	2.353	2.502	2.660	2.826	3.001	3.185	3.379	3.583
8	1.083	1.172	1.267	1.369	1.477	1.594	1.718	1.851	1.993	2.144	2.305	2.476	2.658	2.853	3.059	3.278	3.511	3.759	4.021	4.300
9	1.094	1.195	1.305	1.423	1.551	1.689	1.838-	1.999	2.172	2.358	2.558	2.773	3.004	3.252	3.518	3.803	4.108	4.435	4.785	5.160
10	1.105	1.219	1.344	1.480	1.629	1.791	1.967	2.159	2.367	2.594	2.839	3.106	3.395	3.707	4.046	4.411	4.807	5.234	5.695	6.192
11	1.116	1.243	1.384	1.539	1.710	1.898	2.105	2.332	2.580	2.853	3.152	3.479	3.836	4.226	4.652	5.117	5.624	6.176	6.777	7.430
12	1.127	1.268	1.426	1.601	1.796	2.012	2.252	2.518	2.813	3.138	3.498	3.896	4.335	4.818	5.350	5.936	6.580	7.288	8.064	8.916
13	1.138	1.294	1.469	1.665	1.886	2.133	2.410	2.720	3.066	3.452	3.883	4.363	4.898	5.492	6.153	6.886	7.699	8.599	9.596	10.699
14	1.149	1.319	1.513	1.732	1.980	2.261	2.579	2.937	3.342	3.797	4.310	4.887	5.535	6.261	7.076	7.988	9.007	10.147	11.420	12.839
15	1.161	1.346	1.558	1.801	2.079	2.397	2.759	3.172	3.642	4.177	4.785	5.474	6.254	7.138	8.137	9.266	10.539	11.974	13.590	15.407
16	1.173	1.373	1.605	1.873	2.183	2.540	2.952	3.426	3.970	4.595	5.311	6.130	7.067	8.137	9.358	10.748	12.330	14.129	16.172	18.488
17	1.184	1.400	1.653	1.948	2.292	2.693	3.159	3.700	4.328	5.054	5.895	6.866	7.986	9.276	10.761	12.468	14.426	16.672	19.244	22.186
18	1.196	1.428	1.702	2.026	2.407	2.854	3.380	3.996	4.717	5.560	6.544	7.690	9.024	10.575	12.375	14.463	16.879	19.673	22.901	26.623
19	1.208	1.457	1.754	2.107	2.527	3.026	3.617	4.316	5.142	6.116	7.263	8.613	10.197	12.056	14.232	16.777	19.748	23.214	27.252	31.948
20	1.220	1.486	1.806	2.191	2.653	3.207	3.870	4.661	5.604	6.727	8.062	9.646	11.523	13.743	16.367	19.461	23.106	27.393	32.429	38.338
25	1.282	1.641	2.094	2.666	3.386	4.292	5.427	6.848	8.623	10.835	13.585	17.000	21.231	26.462	32.919	40.874	50.658	62.669	77.388	95.396
30	1.348	1.811	2.427	3.243	4.322	5.743	7.612	10.063	13.268	17.449	22.892	29.960	39.116	50.950	66.212	85.850	111.065	143.371	184.675	237.376
35	1.417	2.000	2.814	3.946	5.516	7.686	10.677	14.785	20.414	28.102	38.575	52.800	72.069	98.100	133.176	180.314	243.503	327.997	440.701	590.668
40	1.489	2.208	3.262	4.801	7.040	10.286	14.974	21.725	31.409	45.259	65.001	93.051	132.782	188.884	267.864	378.721	533.869	750.378	1,051.668	1,469.772
50	1.645	2.692	4.384	7.107	11.467	18.420	29.457	46.902	74.358	117.391	184.565	289.002	450.736	700.233	1,083.657	1,670.704	2,566.215	3,927.357	5,988.914	9,100.438

TABLE B

Present value interest factor of $1 per period at i% for n periods, PVIF(i,n).

Period	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	11%	12%	13%	14%	15%	16%	17%	18%	19%	20%
1	0.990	0.980	0.971	0.962	0.952	0.943	0.935	0.926	0.917	0.909	0.901	0.893	0.885	0.877	0.870	0.862	0.855	0.847	0.840	0.833
2	0.980	0.961	0.943	0.925	0.907	0.890	0.873	0.857	0.842	0.826	0.812	0.797	0.783	0.769	0.756	0.743	0.731	0.718	0.706	0.694
3	0.971	0.942	0.915	0.889	0.864	0.840	0.816	0.794	0.772	0.751	0.731	0.712	0.693	0.675	0.658	0.641	0.624	0.609	0.593	0.579
4	0.961	0.924	0.888	0.855	0.823	0.792	0.763	0.735	0.708	0.683	0.659	0.636	0.613	0.592	0.572	0.552	0.534	0.516	0.499	0.482
5	0.951	0.906	0.863	0.822	0.784	0.747	0.713	0.681	0.650	0.621	0.593	0.567	0.543	0.519	0.497	0.476	0.456	0.437	0.419	0.402
6	0.942	0.888	0.837	0.790	0.746	0.705	0.666	0.630	0.596	0.564	0.535	0.507	0.480	0.456	0.432	0.410	0.390	0.370	0.352	0.335
7	0.933	0.871	0.813	0.760	0.711	0.665	0.623	0.583	0.547	0.513	0.482	0.452	0.425	0.400	0.376	0.354	0.333	0.314	0.296	0.279
8	0.923	0.853	0.789	0.731	0.677	0.627	0.582	0.540	0.502	0.467	0.434	0.404	0.376	0.351	0.327	0.305	0.285	0.266	0.249	0.233
9	0.914	0.837	0.766	0.703	0.645	0.592	0.544	0.500	0.460	0.424	0.391	0.361	0.333	0.308	0.284	0.263	0.243	0.225	0.209	0.194
10	0.905	0.820	0.744	0.676	0.614	0.558	0.508	0.463	0.422	0.386	0.352	0.322	0.295	0.270	0.247	0.227	0.208	0.191	0.176	0.162
11	0.896	0.804	0.722	0.650	0.585	0.527	0.475	0.429	0.388	0.350	0.317	0.287	0.261	0.237	0.215	0.195	0.178	0.162	0.148	0.135
12	0.887	0.788	0.701	0.625	0.557	0.497	0.444	0.397	0.356	0.319	0.286	0.257	0.231	0.208	0.187	0.168	0.152	0.137	0.124	0.112
13	0.879	0.773	0.681	0.601	0.530	0.469	0.415	0.368	0.326	0.290	0.258	0.229	0.204	0.182	0.163	0.145	0.130	0.116	0.104	0.093
14	0.870	0.758	0.661	0.577	0.505	0.442	0.388	0.340	0.299	0.263	0.232	0.205	0.181	0.160	0.141	0.125	0.111	0.099	0.088	0.078
15	0.861	0.743	0.642	0.555	0.481	0.417	0.362	0.315	0.275	0.239	0.209	0.183	0.160	0.140	0.123	0.108	0.095	0.084	0.074	0.065
16	0.853	0.728	0.623	0.534	0.458	0.394	0.339	0.292	0.252	0.218	0.188	0.163	0.141	0.123	0.107	0.093	0.081	0.071	0.062	0.054
17	0.844	0.714	0.605	0.513	0.436	0.371	0.317	0.270	0.231	0.198	0.170	0.146	0.125	0.108	0.093	0.080	0.069	0.060	0.052	0.045
18	0.836	0.700	0.587	0.494	0.416	0.350	0.296	0.250	0.212	0.180	0.153	0.130	0.111	0.095	0.081	0.069	0.059	0.051	0.044	0.038
19	0.828	0.686	0.570	0.475	0.396	0.331	0.277	0.232	0.194	0.164	0.138	0.116	0.098	0.083	0.070	0.060	0.051	0.043	0.037	0.031
20	0.820	0.673	0.554	0.456	0.377	0.312	0.258	0.215	0.178	0.149	0.124	0.104	0.087	0.073	0.061	0.051	0.043	0.037	0.031	0.026
25	0.780	0.610	0.478	0.375	0.295	0.233	0.184	0.146	0.116	0.092	0.074	0.059	0.047	0.038	0.030	0.024	0.020	0.016	0.013	0.010
30	0.742	0.552	0.412	0.308	0.231	0.174	0.131	0.099	0.075	0.057	0.044	0.033	0.026	0.020	0.015	0.012	0.009	0.007	0.005	0.004
35	0.706	0.500	0.355	0.253	0.181	0.130	0.094	0.068	0.049	0.036	0.026	0.019	0.014	0.010	0.008	0.006	0.004	0.003	0.002	0.002
40	0.672	0.453	0.307	0.208	0.142	0.097	0.067	0.046	0.032	0.022	0.015	0.011	0.008	0.005	0.004	0.003	0.002	0.001	0.001	0.001
50	0.608	0.372	0.228	0.141	0.087	0.054	0.034	0.021	0.013	0.009	0.005	0.003	0.002	0.001	0.001	0.001	0.000	0.000	0.000	0.000

TABLE C

Future value interest factor of an ordinary annuity of $1 per period at i% for n periods, FVIFA(i,n).

Period	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	11%	12%	13%	14%	15%	16%	17%	18%	19%	20%
1	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000	1.000
2	2.010	2.020	2.030	2.040	2.050	2.060	2.070	2.080	2.090	2.100	2.110	2.120	2.130	2.140	2.150	2.160	2.170	2.180	2.190	2.200
3	3.030	3.060	3.091	3.122	3.153	3.184	3.215	3.246	3.278	3.310	3.342	3.374	3.407	3.440	3.473	3.506	3.539	3.572	3.606	3.640
4	4.060	4.122	4.184	4.246	4.310	4.375	4.440	4.506	4.573	4.641	4.710	4.779	4.850	4.921	4.993	5.066	5.141	5.215	5.291	5.368
5	5.101	5.204	5.309	5.416	5.526	5.637	5.751	5.867	5.985	6.105	6.228	6.353	6.480	6.610	6.742	6.877	7.014	7.154	7.297	7.442
6	6.152	6.308	6.468	6.633	6.802	6.975	7.153	7.336	7.523	7.716	7.913	8.115	8.323	8.536	8.754	8.977	9.207	9.442	9.683	9.930
7	7.214	7.434	7.662	7.898	8.142	8.394	8.654	8.923	9.200	9.487	9.783	10.089	10.405	10.730	11.067	11.414	11.772	12.142	12.523	12.916
8	8.286	8.583	8.892	9.214	9.549	9.897	10.260	10.637	11.028	11.436	11.859	12.300	12.757	13.233	13.727	14.240	14.773	15.327	15.902	16.499
9	9.369	9.755	10.159	10.583	11.027	11.491	11.978	12.488	13.021	13.579	14.164	14.776	15.416	16.085	16.786	17.519	18.285	19.086	19.923	20.799
10	10.462	10.950	11.464	12.006	12.578	13.181	13.816	14.487	15.193	15.937	16.722	17.549	18.420	19.337	20.304	21.321	22.393	23.521	24.709	25.959
11	11.567	12.169	12.808	13.486	14.207	14.972	15.784	16.645	17.560	18.531	19.561	20.655	21.814	23.045	24.349	25.733	27.200	28.755	30.404	32.150
12	12.683	13.412	14.192	15.026	15.917	16.870	17.888	18.977	20.141	21.384	22.713	24.133	25.650	27.271	29.002	30.850	32.824	34.931	37.180	39.581
13	13.809	14.680	15.618	16.627	17.713	18.882	20.141	21.495	22.953	24.523	26.212	28.029	29.985	32.089	34.352	36.786	39.404	42.219	45.244	48.497
14	14.947	15.974	17.086	18.292	19.599	21.015	22.550	24.215	26.019	27.975	30.095	32.393	34.883	37.581	40.505	43.672	47.103	50.818	54.841	59.196
15	16.097	17.293	18.599	20.024	21.579	23.276	25.129	27.152	29.361	31.772	34.405	37.280	40.417	43.842	47.580	51.660	56.110	60.965	66.261	72.035
16	17.258	18.639	20.157	21.825	23.657	25.673	27.888	30.324	33.003	35.950	39.190	42.753	46.672	50.980	55.717	60.925	66.649	72.939	79.850	87.442
17	18.430	20.012	21.762	23.698	25.840	28.213	30.840	33.750	36.974	40.545	44.501	48.884	53.739	59.118	65.075	71.673	78.979	87.068	96.022	105.93
18	19.615	21.412	23.414	25.645	28.132	30.906	33.999	37.450	41.301	45.599	50.396	55.750	61.725	68.394	75.836	84.141	93.406	103.74	115.27	128.12
19	20.811	22.841	25.117	27.671	30.539	33.760	37.379	41.446	46.018	51.159	56.939	63.440	70.749	78.969	88.212	98.603	110.28	123.41	138.17	154.74
20	22.019	24.297	26.870	29.778	33.066	36.786	40.995	45.762	51.160	57.275	64.203	72.052	80.947	91.025	102.44	115.38	130.03	146.63	165.42	186.69
25	28.243	32.030	36.459	41.646	47.727	54.865	63.249	73.106	84.701	98.347	114.41	133.33	155.62	181.87	212.79	249.21	292.10	342.60	402.04	471.98
30	34.785	40.568	47.575	56.085	66.439	79.058	94.461	113.28	136.31	164.49	199.02	241.33	293.20	356.79	434.75	530.31	647.44	790.95	966.71	1,181.9
35	41.660	49.994	60.462	73.652	90.320	111.43	138.24	172.32	215.71	271.02	341.59	431.66	546.68	693.57	881.17	1,120.7	1,426.5	1,816.7	2,314.2	2,948.3
40	48.886	60.402	75.401	95.026	120.80	154.76	199.64	259.06	337.88	442.59	581.83	767.09	1,013.7	1,342.0	1,779.1	2,360.8	3,134.5	4,163.2	5,529.8	7,343.9
50	64.463	84.579	112.80	152.67	209.35	290.34	406.53	573.77	815.08	1,163.9	1,668.8	2,400.0	3,459.5	4,994.5	7,217.7	10,436	15,090	21,813	31,515	45,497

TABLE D

Present value interest factor of an (ordinary) annuity of $1 per period at i% for n periods, PVIFA(i,n).

Period	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%	11%	12%	13%	14%	15%	16%	17%	18%	19%	20%	21%	22%	23%
1	0.990	0.980	0.971	0.962	0.952	0.943	0.935	0.926	0.917	0.909	0.901	0.893	0.885	0.877	0.870	0.862	0.855	0.847	0.840	0.833	0.826	0.820	0.813
2	1.970	1.942	1.913	1.886	1.859	1.833	1.808	1.783	1.759	1.736	1.713	1.690	1.668	1.647	1.626	1.605	1.585	1.566	1.547	1.528	1.509	1.492	1.474
3	2.941	2.884	2.829	2.775	2.723	2.673	2.624	2.577	2.531	2.487	2.444	2.402	2.361	2.322	2.283	2.246	2.210	2.174	2.140	2.106	2.074	2.042	2.011
4	3.902	3.808	3.717	3.630	3.546	3.465	3.387	3.312	3.240	3.170	3.102	3.037	2.974	2.914	2.855	2.798	2.743	2.690	2.639	2.589	2.540	2.494	2.448
5	4.853	4.713	4.580	4.452	4.329	4.212	4.100	3.993	3.890	3.791	3.696	3.605	3.517	3.433	3.352	3.274	3.199	3.127	3.058	2.991	2.926	2.864	2.803
6	5.795	5.601	5.417	5.242	5.076	4.917	4.767	4.623	4.486	4.355	4.231	4.111	3.998	3.889	3.784	3.685	3.589	3.498	3.410	3.326	3.245	3.167	3.092
7	6.728	6.472	6.230	6.002	5.786	5.582	5.389	5.206	5.033	4.868	4.712	4.564	4.423	4.288	4.160	4.039	3.922	3.812	3.706	3.605	3.508	3.416	3.327
8	7.652	7.325	7.020	6.733	6.463	6.210	5.971	5.747	5.535	5.335	5.146	4.968	4.799	4.639	4.487	4.344	4.207	4.078	3.954	3.837	3.726	3.619	3.518
9	8.566	8.162	7.786	7.435	7.108	6.802	6.515	6.247	5.995	5.759	5.537	5.328	5.132	4.946	4.772	4.607	4.451	4.303	4.163	4.031	3.905	3.786	3.673
10	9.471	8.983	8.530	8.111	7.722	7.360	7.024	6.710	6.418	6.145	5.889	5.650	5.426	5.216	5.019	4.833	4.659	4.494	4.339	4.192	4.054	3.923	3.799
11	10.368	9.787	9.253	8.760	8.306	7.887	7.499	7.139	6.805	6.495	6.207	5.938	5.687	5.453	5.234	5.029	4.836	4.656	4.486	4.327	4.177	4.035	3.902
12	11.255	10.575	9.954	9.385	8.863	8.384	7.943	7.536	7.161	6.814	6.492	6.194	5.918	5.660	5.421	5.197	4.988	4.793	4.611	4.439	4.278	4.127	3.985
13	12.134	11.348	10.635	9.986	9.394	8.853	8.358	7.904	7.487	7.103	6.750	6.424	6.122	5.842	5.583	5.342	5.118	4.910	4.715	4.533	4.362	4.203	4.053
14	13.004	12.106	11.296	10.563	9.899	9.295	8.745	8.244	7.786	7.367	6.982	6.628	6.302	6.002	5.724	5.468	5.229	5.008	4.802	4.611	4.432	4.265	4.108
15	13.865	12.849	11.938	11.118	10.380	9.712	9.108	8.559	8.061	7.606	7.191	6.811	6.462	6.142	5.847	5.575	5.324	5.092	4.876	4.675	4.489	4.315	4.153
16	14.718	13.578	12.561	11.652	10.838	10.106	9.447	8.851	8.313	7.824	7.379	6.974	6.604	6.265	5.954	5.668	5.405	5.162	4.938	4.730	4.536	4.357	4.189
17	15.562	14.292	13.166	12.166	11.274	10.477	9.763	9.122	8.544	8.022	7.549	7.120	6.729	6.373	6.047	5.749	5.475	5.222	4.990	4.775	4.576	4.391	4.219
18	16.398	14.992	13.754	12.659	11.690	10.828	10.059	9.372	8.756	8.201	7.702	7.250	6.840	6.467	6.128	5.818	5.534	5.273	5.033	4.812	4.608	4.419	4.243
19	17.226	15.678	14.324	13.134	12.085	11.158	10.336	9.604	8.950	8.365	7.839	7.366	6.938	6.550	6.198	5.877	5.584	5.316	5.070	4.843	4.635	4.442	4.263
20	18.046	16.351	14.877	13.590	12.462	11.470	10.594	9.818	9.129	8.514	7.963	7.469	7.025	6.623	6.259	5.929	5.628	5.353	5.101	4.870	4.657	4.460	4.279
25	22.023	19.523	17.413	15.622	14.094	12.783	11.654	10.675	9.823	9.077	8.422	7.843	7.330	6.873	6.464	6.097	5.766	5.467	5.195	4.948	4.721	4.514	4.328
30	25.808	22.396	19.600	17.292	15.372	13.765	12.409	11.258	10.274	9.427	8.694	8.055	7.496	7.003	6.566	6.177	5.829	5.517	5.235	4.979	4.746	4.534	4.339
35	29.409	24.999	21.487	18.665	16.374	14.498	12.948	11.655	10.567	9.644	8.855	8.176	7.586	7.070	6.617	6.215	5.858	5.539	5.251	4.992	4.756	4.541	4.348
40	32.835	27.355	23.115	19.793	17.159	15.046	13.332	11.925	10.757	9.779	8.951	8.244	7.634	7.105	6.642	6.233	5.871	5.548	5.258	4.997	4.760	4.544	4.347
50	39.196	31.424	25.730	21.482	18.256	15.762	13.801	12.233	10.962	9.915	9.042	8.304	7.675	7.133	6.661	6.246	5.880	5.554	5.262	4.999	4.762	4.545	4.348