חAmIBIA UחIVERSITY
OF SCIEПCE AПD TECHПOLOGY

## FACULTY OF MANAGEMENT SCIENCES

DEPARTMENT OF ACCOUNTING, ECONOMICS AND FINANCE

| QUALIFICATION: BACHELOR OF ECONOMICS |  |
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| QUALIFICATION CODE: 12BECO | LEVEL: 7 |
| COURSE CODE: MEC712S | COURSE NAME: MATHEMATICAL ECONOMICS |
| SESSION: JANUARY 2024 | PAPER: THEORY |
| DURATION: 3 HOURS | MARKS: 100 |


| SECOND OPPORTUNITY EXAMINATION QUESTION PAPER |  |
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| EXAMINER(S) |  |
|  | MR EDEN TATE SHIPANGA |
| MODERATOR: | DR R. KAMATI |

## INSTRUCTIONS

4. Answer ALL the questions.
5. Write clearly and neatly.
6. Number the answers clearly.

## PERMISSIBLE MATERIALS

4. PEN,
5. PENCIL
6. CALCULATOR

THIS QUESTION PAPER CONSISTS OF 2 PAGES (Including this front page)

## Question 1 [25 Marks]

Consider the following simple one commodity market model:
$Q=b-a P$
$(a, b>0)$
[demand]
$Q=-d+c P$
$(c, d>0)$
[supply]

1. Find the Equilibrium Price $\mathrm{P}^{*}$ and Quantity $\mathrm{Q}^{*}$ ?
2. Use partial derivative to find the effect of the parameters ( $\mathrm{a}, \mathrm{b}, \mathrm{c}$ and d ) on the equilibrium quantity? (15)

## Question 2 [25 Marks]

Consider the following microeconomic model.

$$
\left.\begin{array}{ll}
Q_{d}=D\left(P, Y_{0}\right) & {\left[D_{P}<0 ; D_{Y_{0}}>0\right]} \\
Q_{s}=D\left(P, T_{0}\right) & {\left[S_{P}>0 ;\right.}
\end{array} S_{T_{0}}<0\right] ~ \$
$$

Where $Y_{0}$ is income and $T_{0}$ is the tax on the commodity.
Analyse the comparative statics of the model to find the effect of change in Income and Tax on the equilibrium Q and P ?

## Question 3 [25 Marks]

Give the input matrix and the final demand vector

$$
A=\left[\begin{array}{ccc}
0.05 & 0.25 & 0.34 \\
0.33 & 0.10 & 0.12 \\
0.19 & 0.38 & 0
\end{array}\right] \quad d=\left[\begin{array}{c}
1800 \\
200 \\
900
\end{array}\right]
$$

(a) Explain the economic meaning of the elements $0.33,0$ and 200
(b) Explain the economic meaning (if any) of the third column sum
(c) Find the solution output levels by Cramer's rule

## Question 4 [25 Marks]

1. Optimise the following function, a) find the critical value for the first order condition and b) the high-order Hessian:

$$
\begin{equation*}
y=4 x_{1}^{2}-7 x_{1}-x_{1} x_{2}+8 x_{2}^{2}-5 x_{2}+2 x_{2} x_{3}+4 x_{3}^{2}+2 x_{3}-4 x_{1} x_{3} \tag{15}
\end{equation*}
$$

2. Use discriminants to determine whether each of the following quadratic function is positive or negative definite:

$$
\begin{equation*}
y=5 x_{1}^{2}-6 x_{1} x_{2}+3 x_{2}^{2}-2 x_{2} x_{3}+8 x_{3}^{2}-3 x_{1} x_{3} \tag{10}
\end{equation*}
$$

