

Faculty of Health, Natural **Resources and Applied Sciences** 

School of Natural and Applied Sciences

Department of Mathematics, Statistics and Actuarial Science

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QUALIFICATION: BACHELOR of SCIENCE IN APPLIED MATHEMATICS AND STATISTICS & BACHELOR of SCIENCE							
QUALIFICATION CODE: 07BSAM & 07BSOC	LEVEL: 5						
COURSE: INTRODUCTION TO APPLIED STATISTICS COURSE CODE: IASS							
DATE: NOVEMBER 2024	SESSION: 1						
DURATION: 3 HOURS	MARKS: 100						

FIRST OPPORTUNITY: EXAMINATION QUESTION PAPER

**EXAMINER:** 

MR. ANDREW ROUX

MODERATOR:

DR. DISMAS NTIRAMPEBA

#### **INSTRUCTIONS**

- 1. Answer all questions on the separate answer sheet.
- 2. Please write neatly and legibly.
- 3. Do not use the left side margin of the exam paper. This must be allowed for the examiner.
- 4. No books, notes and other additional aids are allowed.
- 5. Mark all answers clearly with their respective question numbers.

#### PERMISSIBLE MATERIALS:

Non-Programmable Calculator

#### **ATTACHEMENTS**

- 1. Statistical Formulae Sheet
- 2. Standard Normal Probability Distribution Table
- 3. 1 x A4 Graph Sheet

This paper consists of 7 pages including this front page

#### QUESTION 1 [10 x 2 = 20]

## Write down the letter corresponding to your choice next to the question number

1.1)	Which of the following methods are used in analysing categorical (qualitati data	ve) (2)
	A. Bar charts, pie charts and Histogram	
	B. Bar charts, pie charts and frequency tables	
	C. Mean, median and mode  D. Variance, standard deviation and coefficient of variation	
	E. None of the above	
1.2)	In a positively skewed distribution, the mean is	(2)
	A. below the median	
	B. above the median	
	C. equal to the median	
	D. below the mode	
	E. none of the above	
1.3)	Which of the following are measures of dispersion (spread)	(2)
	A. Range, Variance and Standard deviation	
	B. Range, mean, median and mode	
	C. Mean, median and mode	
	D. Quartile, Decile and percentile	
	E. Mean, median and percentile	
1.4)	Censuses are rarely done as compared to sample surveys because:	(2)
	A. Sample surveys can be done in a short time as compared to censuses B. Sample surveys are cheap to implement as compared to censuses C. Sample surveys are easy to implement as compared to censuses D. All of the above	

1.5)	Fill in the blank to make t	: "Theof a								
	particular outcome is the a population ."	number of times it occurs	within a specific sample of (2)							
	A. Frequency	B. Variance								
	C. Mean deviation	D. Distribution								
	E. Mean									
1.6)	A Sample of a population	is:	(2)							
	A. A subset of the popula B. An experiment in the p C. An outcome of the popul D. A variable in the popul E. All of the above	opulation pulation								
1.7)	Height is a	measurement scal	e variable (2)							
	A. Ordinal	B. Interval	C. Ratio							
	D. Nominal	E. None of the above								
1.8)	Consider the shoes size of	of 12 students at NUST:	(2)							
	4, 6, 12, 7, 9, 7, 8, 11, 8,	8, 11, 5								
	Which of the following ar	nswers is incorrect?								
	A. This is a bimodal distri B. The range of this data C. The modal shoes size D. The lowest value of thi E.The median of this data	values is 8. is 8. s data values is 4.								
1.9)	Which of the following sta	tements is not true about	the mean? (2)							
	A. The value of the mean the of all observations	times the number of obse	rvations equals the sum of							
	B. It utilizes all values in	its calculation								
	C. It is not affected by ex	treme values (outliers)								
	D. It is the best measure of central tendency when the data is not skewed									
	E. In a symmetric distribu equal	tion, the mean, the mediar	and the mode are all							

1.10) A list of 5 pulse rates is: 70, 64, 80, 74, 92. What is the median for this list? (2)

A. 74

B. 76

C. 77 D. 80

E. None of the provided

#### QUESTION 2 [28]

A variable is normally distributed with mean 6 and standard deviation 2. Find the probability that the variable will

2.1.1) lie between 1 and 7 (inclusive).

(4)

2.1.2) at least 5.

(4)

2.1.3) at most 4

(4)

2.2)The Namibia Cycling Federation has revealed that only 12 out of every 20 cyclist successfully finish the Desert Dash. Based upon this assumption, determine the probability that out of a random sample of 5 cyclists

2.2.1) None of them will successfully finish the Desert Dash

(3)

2.2.2) All of them will successfully finish the Desert Dash

(3)

2.2.3) At least one of them will successfully finish the Desert Dash 2.2.4) At most one of them will successfully finish the Desert Dash (5)

(5)

#### QUESTION 3 [15]

Below are prices of toothpaste, shampoo, cough tablets, and antiperspirant for August 2020 and August 2023. Also included are quantities purchased.

	August		-			
	2020		August2023			
Item	Price	Quantity	Price	Quantity		
Toothpaste	2.49	6	2.69	6		
Shampoo	3.29	4	3.59	5		
Cough tablets	1.59	2	1.79	3		
Antiperspirant	1.79	3	2.29	4		

3.1) Use 2020 as the base period to compute and interpret the simple price index

in 2023 for

- 3.1.1 toothpaste (2)
- 3.1.2 shampoo (2)
- 3.2) Construct a price index to reflect the overall change in prices of the items purchased for the period 2020 2023. Use the Laspeyres approach. Interpret your price index. (6)
- 3.3) Calculate and interpret the unweighted aggregate price index for 2023 on 2020 as base year. (5)

#### QUESTION 4 [15]

The table below shows the annual rainfall (x 100 mm) recorded during the last decade at the Goabeb Research Station in the Namib Desert

Year	Rainfall
2014	3.0
2015	4.2
2016	4.8
2017	3.7
2018	3.4
2019	4.3
2020	5.6
2021	4.4
2022	3.8
2023	4.1

4.1 Construct a scatter plot

- (4)
- 4.2 Determine the least squares trend line equation, using the sequential coding method with 2014 = 1. (7)
- 4.3 Use the trend line equation obtained in 4.2 to find rainfall for 2012 and 2027 (4)

#### QUESTION 5 [22]

A small lab testing blood samples for multiple comorbidities has kept a record of samples tested for March and June 2022. The samples are summarized in the following frequency distribution:

Samples	Number of days	
60-<70	5	
70-<80	11	
80-<90	22	
90-<100	13	
100-<110	7	
110-<120	3	

- 5.1) Calculate the mean, median and modal number of samples tested between March and June (5 + 5 + 5)
- 5.2) Calculate standard deviation in the number of samples tested between March and June (7)

Xxxxxxxxxxxxxxxxxx

END OF EXAMINATION XXXXXXXXXXXXXXXX

#### **FORMULAE SHEET**

Mean 
$$\bar{x} = \frac{\sum xf}{n}$$
; Mode= $L + \frac{c(f_m - f_{m-1})}{2 \times f_m - f_{m-1} - f_{m+1}}$ ; Median= $L + \frac{c(0.5n - CF)}{f_{me}}$ 

$$\beta = \frac{n(\sum xy) - (\sum x)(\sum y)}{n(\sum x^2) - (\sum x)^2} \quad ; \qquad \alpha = \frac{\sum y - \beta(\sum x)}{n}$$

$$\operatorname{Mean} \, \bar{x} = \frac{\sum xf}{n} \, ; \operatorname{Mode} = L + \frac{c(f_m - f_{m-1})}{2 \times f_m - f_{m-1} - f_{m+1}} \quad ; \quad \operatorname{Median} = L + \frac{c(0.5n - CF)}{f_{me}}$$

$$\beta = \frac{n(\sum xy) - (\sum x)(\sum y)}{n(\sum x^2) - (\sum x)^2} \quad ; \quad \alpha = \frac{\sum y - \beta(\sum x)}{n}$$

$$Ip(L) \frac{\sum P_i \times Q_b}{\sum P_b \times Q_b} \times 100 \quad ; \quad Ip(P) = \frac{\sum P_i \times Q_i}{\sum P_b \times Q_i} \times 100 \quad ;$$

$$Ip = \frac{\sum p_1}{\sum p_0} \times 100\%$$

$$Var(x) = \frac{\sum X^2 - n(\bar{x})^2}{n - 1} \quad ; \quad Std \; Dev, \; s = \sqrt{Var(x)} \quad ;$$

$$CV = \frac{Std \; Dev}{\bar{x}} \; x \; 100 \quad ;$$

$$Var(x) = \frac{\sum X^{2} - n(\overline{x})^{2}}{n-1} ; Std Dev, s = \sqrt{Var(x)} ;$$

$$CV = \frac{Std Dev}{\overline{x}} x 100 ;$$

#### Z - Table

The table shows cumulative probabilities for the standard normal curve.

# Cumulative probabilities for NEGATIVE z-values are shown first. SCROLL DOWN to the $2^{nd}$ page for POSITIVE z

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
-3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
-3.2	.0007	.0007	.0006	.0006	.0006	.0006	.0006	.0005	.0005	.0005
-3.1	.0010	.0009	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.0007
-3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0011	.0010	.0010
-2.9	.0019	.0018	.0018	.0017	.0016	.0016	.0015	.0015	.0014	.0014
-2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
-2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0026
-2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.0036
-2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.0048
-2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.0064
-2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.0084
-2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.0110
-2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.0143
-2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.0183
-1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.0233
-1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.0294
-1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384	.0375	.0367
-1.6	.0548	.0537	.0526	.0516	.0505	.0495	.0485	.0475	.0465	.0455
-1.5	.0668	.0655	.0643	.0630	.0618	.0606	.0594	.0582	.0571	.0559
-1.4	.0808	.0793	.0778	.0764	.0749	.0735	.0721	.0708	.0694	.0681
-1.3	.0968	.0951	.0934	.0918	.0901	.0885	.0869	.0853	.0838	.0823
-1.2	.1151	.1131	.1112	.1093	.1075	.1056	.1038	.1020	.1003	.0985
-1.1	.1357	.1335	.1314	.1292	.1271	.1251	.1230	.1210	.1190	.1170
-1.0	.1587	.1562	.1539	.1515	.1492	.1469	.1446	.1423	.1401	.1379
-0.9	.1841	.1814	.1788	.1762	.1736	.1711	.1685	.1660	.1635	.1611
-0.8	.2119	.2090	.2061	.2033	.2005	.1977	.1949	.1922	.1894	.1867
-0.7	.2420	.2389	.2358	.2327	.2296	.2266	.2236	.2206	.2177	.2148
-0.6	.2743	.2709	.2676	.2643	.2611	.2578	.2546	.2514	.2483	.2451
-0.5	.3085	.3050	.3015	.2981	.2946	.2912	.2877	.2843	.2810	.2776
-0.4	.3446	.3409	.3372	.3336	.3300	.3264	.3228	.3192	.3156	.3121
-0.3	.3821	.3783	.3745	.3707	.3669	.3632	.3594	.3557	.3520	.3483
-0.2	.4207	.4168	.4129	.4090	.4052	.4013	.3974	.3936	.3897	.3859
-0.1	.4602	.4562	.4522	.4483	.4443	.4404	.4364	.4325	.4286	.4247
0.0	.5000	.4960	.4920	.4880	.4840	.4801	.4761	.4721	.4681	.4641

### Cumulative probabilities for POSITIVE z-values are shown below.

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
0.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
0.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
0.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
0.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998