

## **FACULTY OF MANAGEMENT SCIENCES**

# DEPARTMENT OF ACCOUNTING, ECONOMICS AND FINANCE

QUALIFICATION: BACHELOR OF ECONOMICS	
QUALIFICATION CODE: 12BECO	LEVEL: 7
COURSE CODE: MEC712S	COURSE NAME: MATHEMATICAL ECONOMICS
SESSION: JANUARY 2025	PAPER: THEORY
DURATION: 3 HOURS	MARKS: 100

SECOND OF	PORTUNITY EXAMINATION QUESTION PAPER
EXAMINER(S)	
	MR EDEN TATE SHIPANGA
MODERATOR:	DR R. KAMATI

	INSTRUCTIONS
4.	Answer ALL the questions.
5.	Write clearly and neatly.
6.	Number the answers clearly.

## PERMISSIBLE MATERIALS

- 4. PEN,
- 5. PENCIL
- 6. CALCULATOR

THIS QUESTION PAPER CONSISTS OF 2 PAGES (Including this front page)

## Question 1 [25 Marks]

Consider the following Microeconomic market model, where A is the level of technology.

$$Q = D(P, Y)$$

$$\left[D_P<0,D_Y>0\right]$$

$$Q = S(P, A)$$

$$[S_P > 0; S_A > 0]$$

Analyse the comparative statics of the model to find the effect of the level of technology and Income on the equilibrium quantity and price simultaneously.

(25)

#### Question 2 [25 Marks]

Consider the following simple one commodity market model:

$$Q = b - aP$$

$$Q = -d + cP$$

1. Find the Equilibrium Price P\* and Quantity Q\*?

(10)

2. Use partial derivative to find the effect of the parameters (a, b, c and d) on the equilibrium quantity?

(15)

#### Question 3 [25 Marks]

i. Use Jacobian determinants to test the existence of functional dependence between the paired functions.

a)

$$y_1 = 3x_1^2 + x_2$$

$$y_2 = 9x_1^4 + 6x_1^2(x_2 + 4) + x_2(x_2 + 8) + 12$$
 (5)

b)

$$y_1 = 3x_1^2 + 2x_2^2$$

$$y_2 = 5x_1 + 1 ag{5}$$

ii. Optimise the following function, a) find the critical value for the first order condition and b) the high-order Hessian:

$$y = 4x_1^2 - 7x_1 - x_1x_2 + 8x_2^2 - 5x_2 + 2x_2x_3 + 4x_3^2 + 2x_3 - 4x_1x_3$$
 (15)

#### Question 4 [25 Marks]

Maximise profits using Kuhn-Tucker conditions,  $\pi = 54x - x^2 + 76y - 3y^2 - 12$  subject to the production constraint  $x + y \le 35$  (25)

**TOTAL MARKS: 100**